



THE UNIVERSITY OF BRITISH COLUMBIA

Multiaxial Constitutive and Numerical Modeling in Geo-mechanics within Critical State Theory

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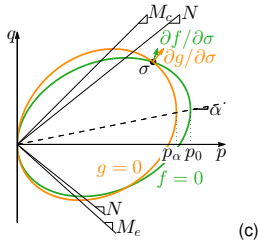


- 1 Constitutive modeling for clays
 - SANICLAY class
 - Model Performance
- 2 Constitutive modeling for sands
 - SANISAND class
 - Model Performance
- 3 Application in numerical modeling
 - Model implementations
 - Nonlinear effective stress seismic site response analysis
- 4 Discussion related to the SCEC workshop

SANICLAY: Simple ANIsotropic CLAY plasticity model

• SANICLAY

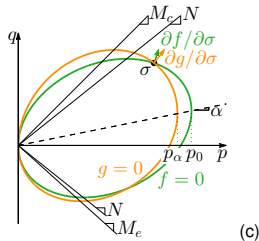
(Dafalias et al., 2006)



SANICLAY: Simple ANIsotropic CLAY plasticity model

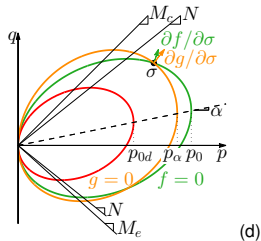
- SANICLAY

(Dafalias et al., 2006)



- SANICLAY-D

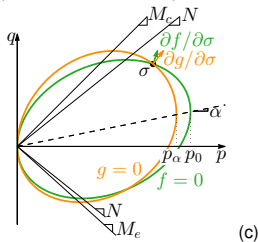
(Taiebat et al., 2010a)



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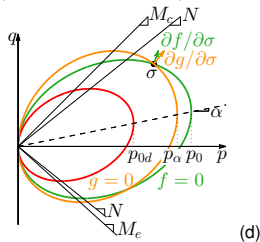
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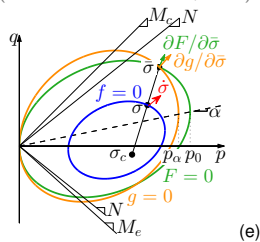
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(Taiebat et al., 2010a)



• SANICLAY-B

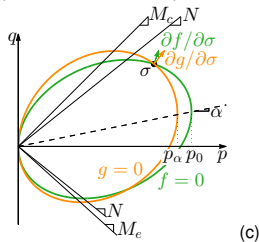
(Seidalinov and Taiebat, 2014)



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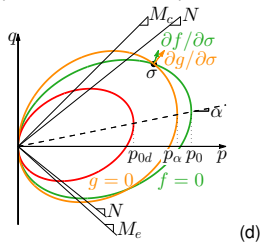
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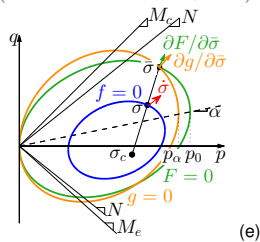
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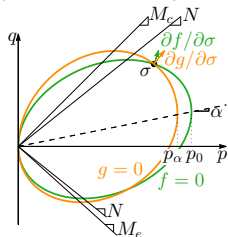


- Systematic tensorial extension to multiaxial stress space

SANICLAY: Simple ANIsotropic CLAY plasticity model

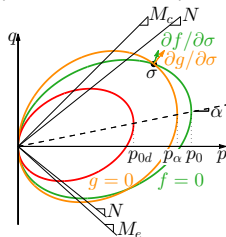
• SANICLAY

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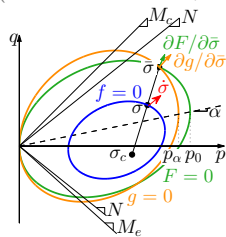
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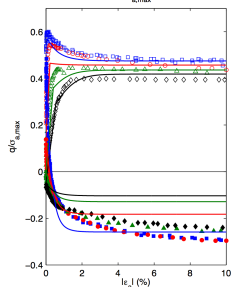
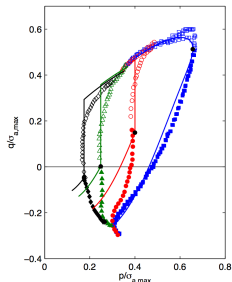


- Systematic tensorial extension to multiaxial stress space
- Relatively straightforward calibration process

	Model constant category	Designation	Georgia kaolin	Cloverdale	Ariake
MCC	Elasticity	κ	0.03	0.037	0.05
		ν	0.2	0.2	0.2
	Critical state	λ	0.21	0.121	0.41
SANICLAY		M_c, M_e	1.29, 1.27	0.87, 0.86	1.68, 1.65
	Yield surface	N	1	0.8	1.68
	Rotational hardening	C	3	3	15
SANICLAY-D		x	1.73	1.69	1.76
	Destructuration	k_i	2	0	0
SANICLAY-B	Bounding surface	h_0	550	50	1600
		a_d	68	7	80

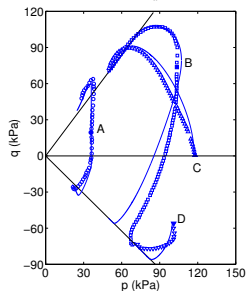
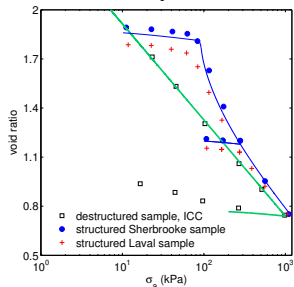
Monotonic loading (iso. comp., oedometer, undrained triaxial comp./ext.)

Lower Cromer Till



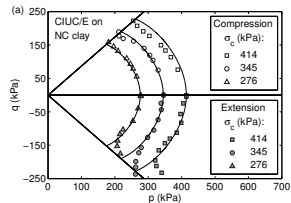
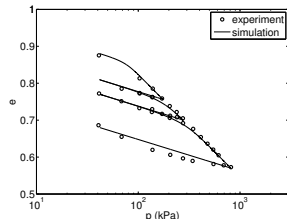
Data: after Gens (1982)

Bothkennar clay



Data: after Smith et al. (1992)

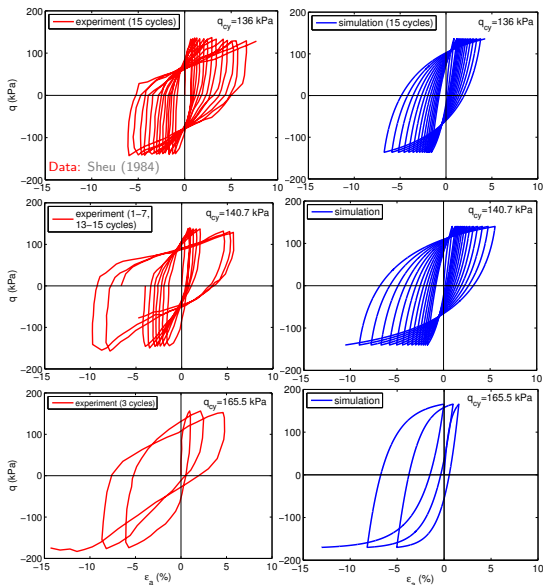
Georgia kaolin clay



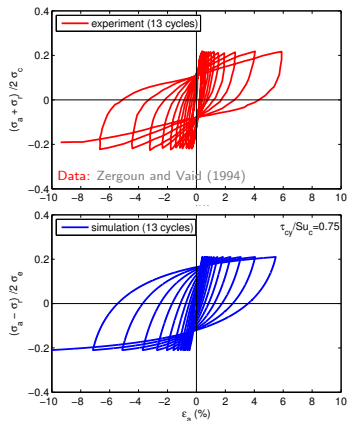
Data: after Sheu (1984)

Undrained cyclic triaxial tests

Georgia kaolin clay (reconstituted)



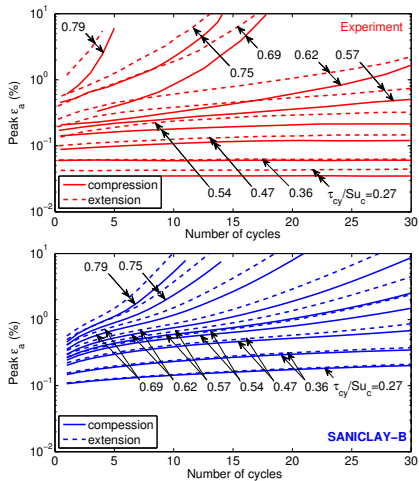
Cloverdale clay (structured)



Simulations: Seidalinov and Taiebat (2014)

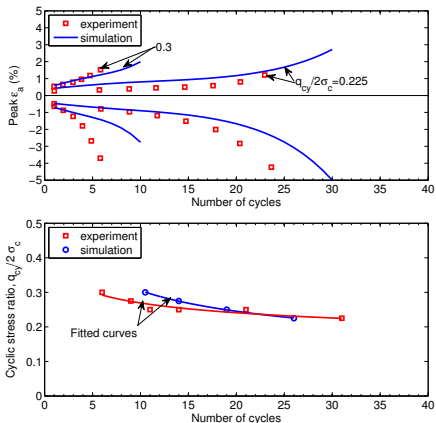
Undrained cyclic triaxial tests

• Cloverdale clay (structured)



Data: Zergoun and Vaid (1994)

• Ariake clay (reconstituted)



Data: Yasuhara et al. (1992)

Simulations: Seidalinov and Taiebat (2014)

SANISAND: Simple ANIsotropic SAND plasticity model

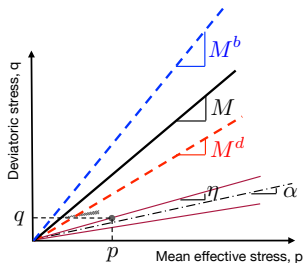
Dafalias, Manzari, Li, Papadimitriou, Taiebat (1997-2012)

- Formulation in triaxial stress space

$$f = |\eta - \alpha| - m = 0 \quad \eta = \frac{q}{p}$$

$$\dot{\varepsilon}_q^p = \frac{\dot{\eta}}{hb} \quad b = (M^b - \eta)$$

$$\dot{\varepsilon}_v^p = A_d d |\dot{\varepsilon}_q^p| \quad d = (M^d - \eta)$$



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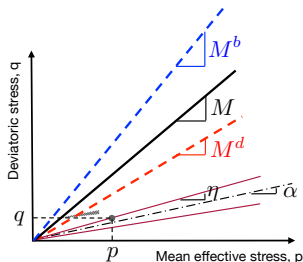
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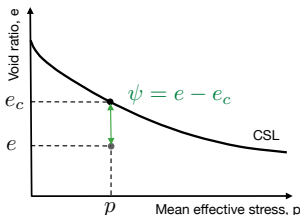
$$\dot{\varepsilon}_v^p = A_d d |\dot{\varepsilon}_q^p| \quad d = (M^d - \eta)$$



- Dependence on state parameter

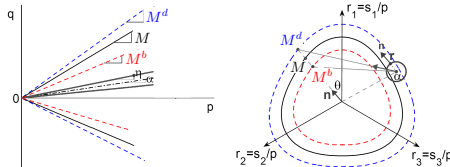
$$M^b = M \exp(-n^b \psi)$$

$$M^d = M \exp(n^d \psi)$$



Generalization and model constants

- Systematic tensorial extension to multiaxial stress space



- Relatively straightforward calibration process

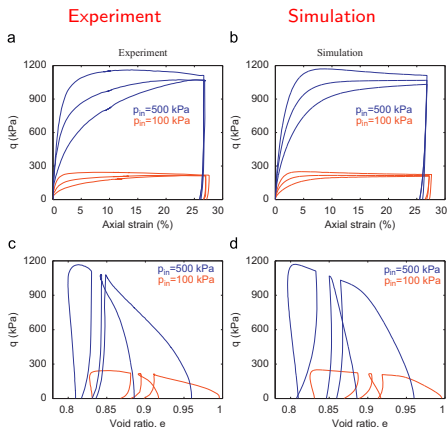
Taiebat et al. (2010b)

Parameter	Symbol	Toyoura	Nevada	Sacramento
Elasticity	G_0	125	150	200
	ν	0.05	0.05	0.2
CSL	M	1.25	1.14	1.35
	c	0.712	0.78	0.65
	e_0	0.934	0.83	0.96
	λ	0.019	0.027	0.028
	ξ	0.7	0.45	0.7
Dilatancy	η^d	2.1	1.05	2.0
	A_0	0.704	0.81	0.8
Kinematic	η^b	1.25	2.56	1.2
Hardening	h_0	7.05	9.7	5.0
	c_h	0.968	1.02	1.03
Fabric dilatancy	$z_{\max}$	2.0	5.0	–
	c_z	600	800	–

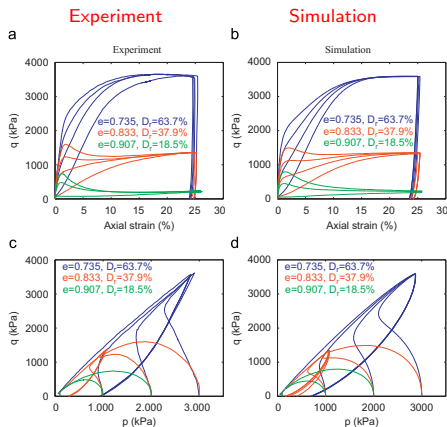
- Soil-specific set of constants for different densities & confining pressures.
- Constitutive ingredients to account for
 - ψ -dependent dilatancy stress-ratio (Manzari and Dafalias, 1997; Li and Dafalias, 2000)
 - evolving fabric anisotropy (Dafalias and Manzari, 2004)
 - inherent fabric anisotropy (Dafalias et al., 2004)
 - plastic strains under const. stress-ratio & particle crushing (Taiebat and Dafalias, 2008)
 - anisotropic critical state (Li and Dafalias, 2012)

Triaxial loading and unloading on Toyoura sand

• Drained triaxial tests



• Undrained triaxial tests



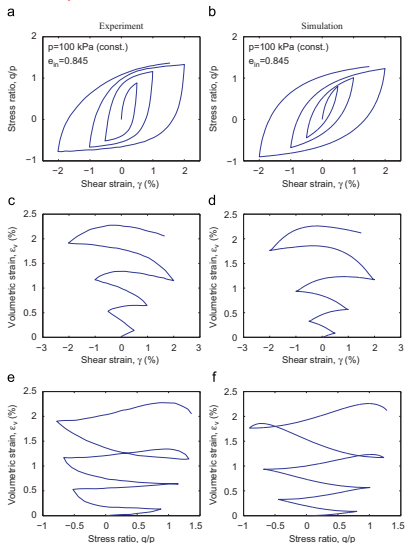
Data: Verdugo and Ishihara (1996); **Simulations:** Taiebat et al. (2010b)

Constant- p cyclic triaxial on Toyoura sand

● Loose sample

Experiment

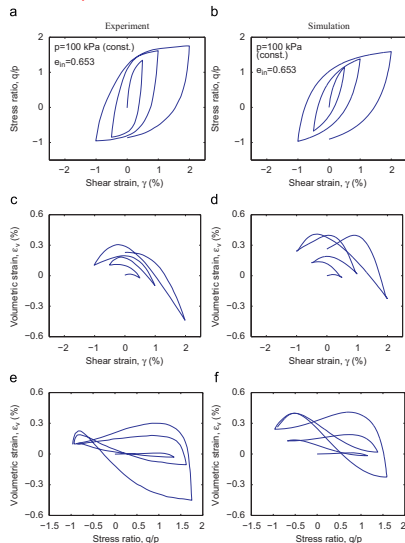
Simulation



● Dense sample

Experiment

Simulation



Data: Pradhan et al. (1989); Simulations: Taiebat et al. (2010b)

Finite Element platform and model implementation

- OpenSees: The Open System for Earthquake Engineering Simulation
 - Fully coupled nonlinear dynamic finite element program
 - Open-source: <http://opensees.berkeley.edu>
 - Variety of relevant element types for continuum modeling of soil medium
 - 2D (quad) and 3D (brick)
 - single phase (solid, u) and double phase (solid and pore fluid, u-p)
 - Variety of analysis types, integration schemes, and solvers

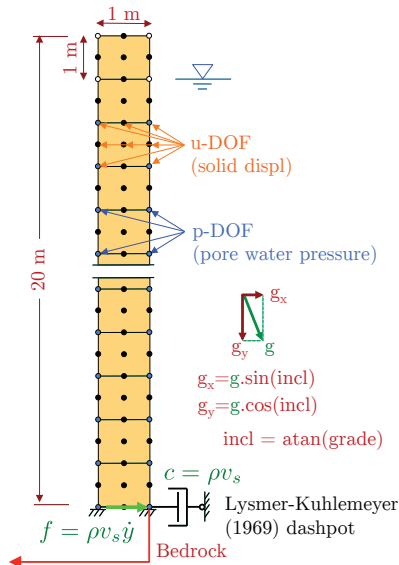
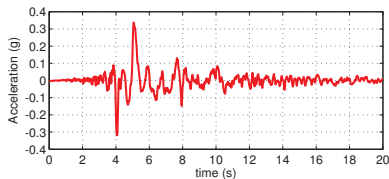
Finite Element platform and model implementation

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 - single phase (solid, u) and double phase (solid and pore fluid, u - p)
 - Variety of analysis types, integration schemes, and solvers
- SANICLAY and SANISAND implementation:
 - SANICLAY: Refined explicit integration scheme with automatic sub-stepping and error control (Seidalinov and Taiebat, 2014)
 - SANISAND: Various explicit and implicit integration schemes (Ghofrani and Arduino, 2014)
 - All implementations are in full tensorial forms of stresses and strains (3D)

Application of SANICLAY models

Modeling of infinite slope subjected to earthquake excitation:

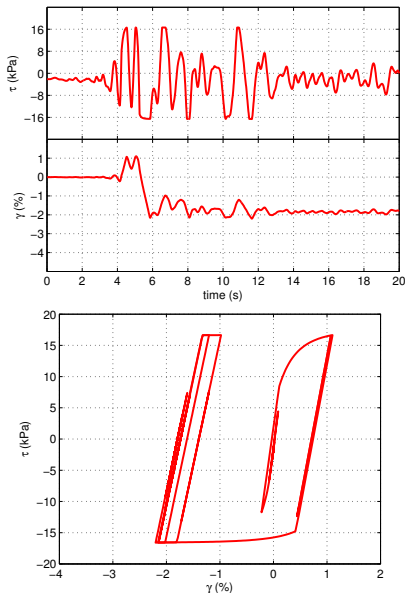
- 20 m deep (2% grade) deposit of NC clay
 - SANICLAY & SANICLAY-B models
 - 1 m water table, permeability: 10^{-8} m/s
 - Periodic BCs to emulate 1D analysis
- Modeling
 - 9-node quad u - p element (Biot's theory)
 - Periodic BCs to emulate 1D analysis
 - Base dashpot to account for the finite rigidity of the underlying elastic medium
 - Velocity time history $\dot{u}(t)$ and high $V_{s,base}$
- Imperial Valley record scaled to $PGA=0.35g$



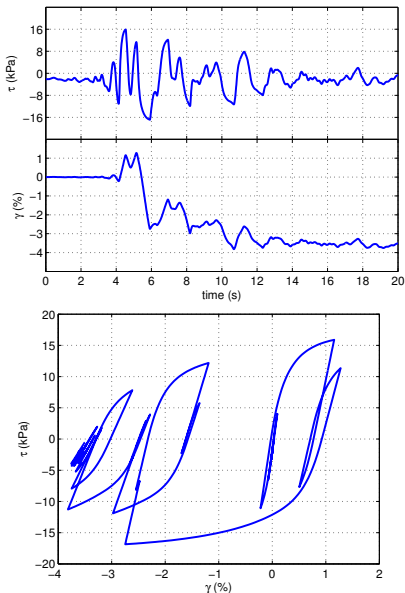
Adopted from McGann and Arduino (2013)

Results: shear stress (τ) & shear strain (γ) at depth of 5.5 m

• SANICLAY

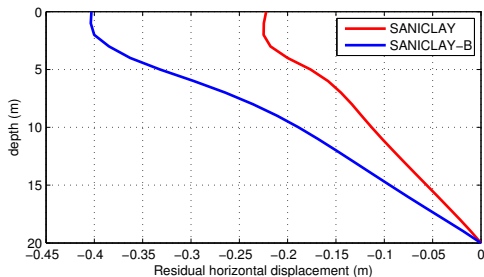


• SANICLAY-B

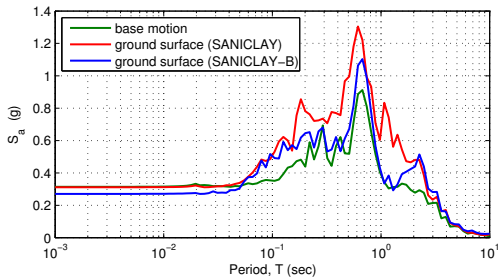


Results: Displacement profile and spectral accelerations

- Horizontal displacement profiles at the end of shaking



- Spectral acceleration at the base and top of soil columns

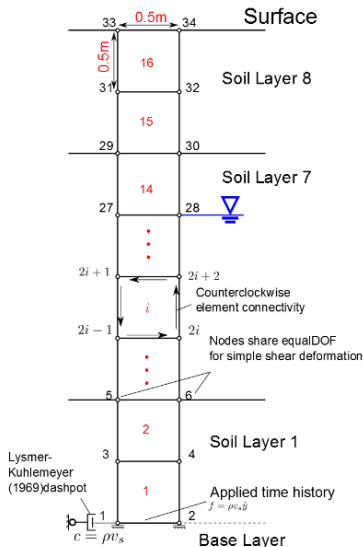


Application of SANISAND model in PRENOLIN

Modeling of free field soil column subjected to earthquake excitation in Sendai:

- 8 m deep deposit of sand
 - 0–7 m: SANISAND, and 7–8 m elastic
 - 1.5 m water table, permeability: 10^{-5} m/s
 - Periodic BCs to emulate 1D analysis
- Modeling
 - SSPquadUP element (Biot's theory)
 - Periodic BCs to emulate 1D analysis
 - Base dashpot to account for the finite rigidity of the underlying elastic medium
 - Velocity time history $\dot{u}(t)$ and high $V_{s,base}$
- Several motions from downhole arrays at Sendai site

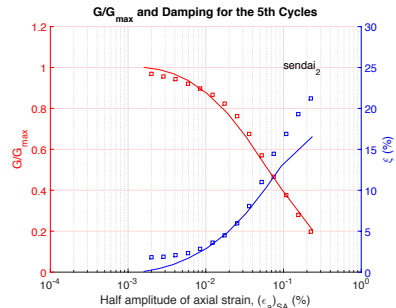
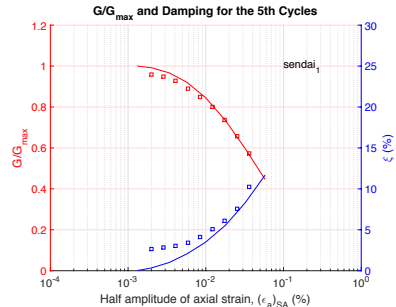
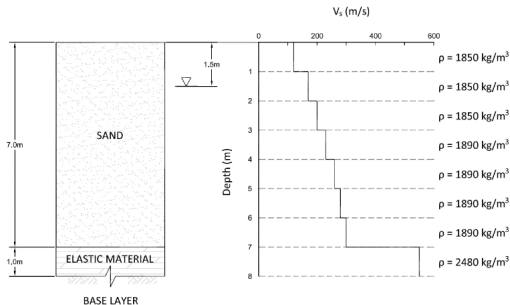
[Collaborative study with UW]



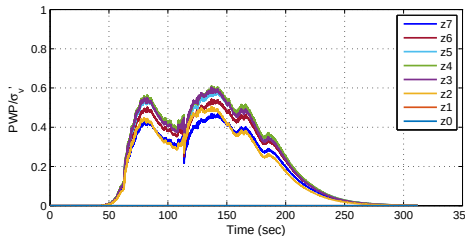
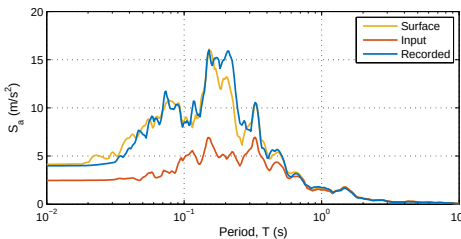
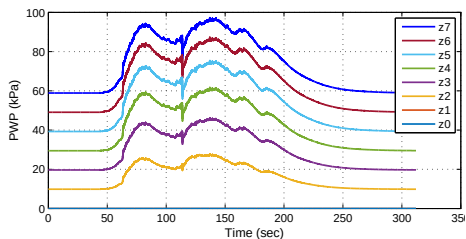
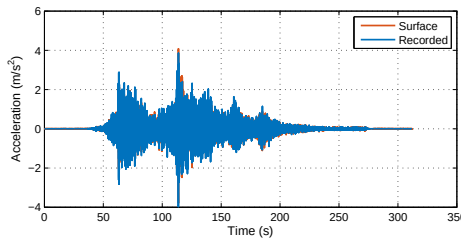
Adopted from McGann and Arduino (2013)

Soil properties

- Calibration based on data of
 - drained monotonic triaxial tests at three different confining pressures
 - undrained cyclic triaxial tests on two frozen samples at depths of 3.5 and 5.5 m, resulting in plots of $G/G_{\max}$ and ξ vs. $(\epsilon_a)_{SA}$
- Stiffness adjusted based on profile of V_s



Analysis results for one of the ground motions

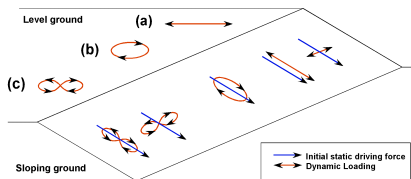


Challenges for 3D seismic site response?!

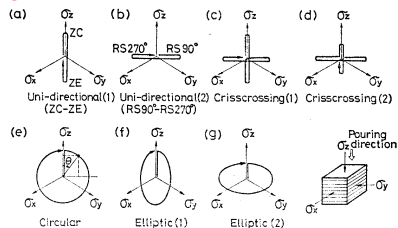
- Moving from 1D to 3D in regional-scale simulations:
 - Our models have always been 3D ✓
 - 3D is the same in any scale and our scale is that of continuum ✓

Challenges for 3D seismic site response?!

- Moving from 1D to 3D in regional-scale simulations:
 - Our models have always been 3D ✓
 - 3D is the same in any scale and our scale is that of continuum ✓
- Further works in constitutive modeling
 - Fabric-related strongly anisotropic response (next slide)
 - Constitutive modeling of intermediate soils ...
 - Validating the models for multiaxial loading ...



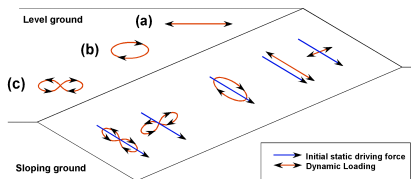
Kammerer (2002)



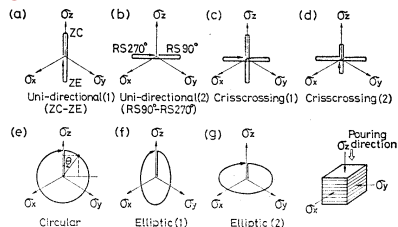
Yamada and Ishihara (1983)

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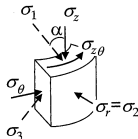
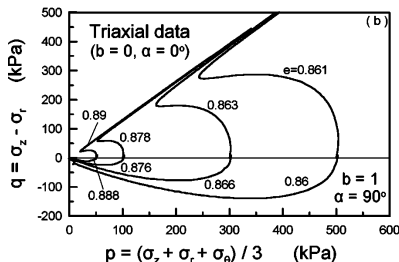
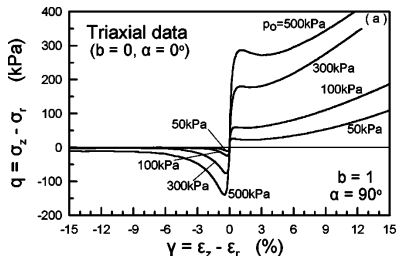
Kammerer (2002)



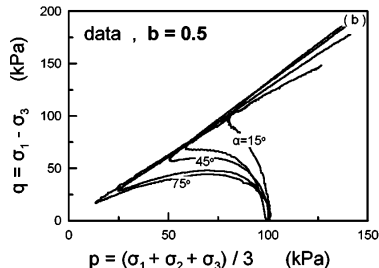
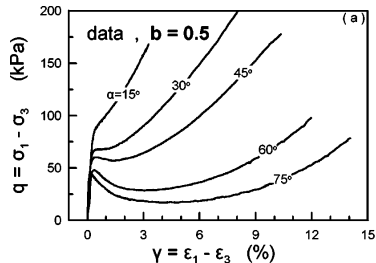
Yamada and Ishihara (1983)

- Calibration and simulation
 - State parameters including internal variables from in-situ testing results?!
 - Statistical methods to deal with scarce and sparse input parameters?!
 - Professional programming and use of HPC techniques?!

Fabric-related strongly anisotropic response



$$b = \frac{\sigma_2 - \sigma_3}{\sigma_1 - \sigma_3}$$



Yoshimine et al. (1998)



THANK YOU!

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- Mr. Gaziz Seidalinov (UBC)
- Mr. Graeme McAllister (UBC)
- Mr. Alborz Ghofrani (UW)
- Mr. Long Chen (UW)

Bibliography I

- Dafalias, Y. F. and Manzari, M. T. (2004), 'Simple plasticity sand model accounting for fabric change effects', *ASCE Journal of Engineering Mechanics* **130**(6), 622–634.
- Dafalias, Y. F., Manzari, M. T. and Papadimitriou, A. G. (2006), 'SANICLAY: simple anisotropic clay plasticity model', *Int'l Journal for Numerical and Analytical Methods in Geomechanics* **30**(12), 1231–1257.
- Dafalias, Y. F., Papadimitriou, A. G. and Li, X. S. (2004), 'Sand plasticity model accounting for inherent fabric anisotropy', *Journal of Engineering Mechanics* **130**(11), 1319–1333.
- Gens, A. (1982), Stress–strain and strength of a low plasticity clay, Ph.D. thesis, Imperial College, London University. 856 pages.
- Kammerer, A. M. (2002), Undrained Response of Monterey 0/30 Sand Under Multidirectional Cyclic Simple Shear Loading Conditions, PhD thesis, University of California, Berkeley.
- Li, X. S. and Dafalias, Y. F. (2000), 'Dilatancy for cohesionless soils', *Géotechnique* **54**(4), 449–460.
- Li, X. S. and Dafalias, Y. F. (2012), 'Anisotropic critical state theory: role of fabric', *Journal of Engineering Mechanics* **138**(3), 263–275.
- Manzari, M. T. and Dafalias, Y. F. (1997), 'A critical state two–surface plasticity model for sands', *Géotechnique* **47**(2), 255–272.
- McGann, C. and Arduino, P. (2013), 'Effective stress site response analysis of a layered soil column'. http://opensees.berkeley.edu/wiki/index.php/Effective_Stress_Site_Response_Analysis_of_a_Layered_Soil_Column.
- Pradhan, T. B., Tatsuoka, F. and Sato, Y. (1989), 'Experimental stress–dilatancy relations of sand subjected to cyclic loading', *Soils and Foundations* **29**(1), 45–64.
- Seidalinov, G. and Taiebat, M. (2014), 'Bounding surface SANICLAY plasticity model for cyclic clay behavior', *International Journal for Numerical and Analytical Methods in Geomechanics* **38**(7), 702–724.

Bibliography II

- Sheu, W. (1984), Modeling of stress-strain-strength behavior of a clay under cyclic loading, Ph.D. dissertation, University of Colorado, Boulder, Colorado, USA.
- Smith, P. R., Jardine, R. J. and Hight, D. W. (1992), 'Yielding of bothkennar clay', *Géotechnique* **42**(2), 257–274.
- Taiebat, M. and Dafalias, Y. F. (2008), 'SANISAND: simple anisotropic sand plasticity model', *International Journal for Numerical and Analytical Methods in Geomechanics* **32**(8), 915–948.
- Taiebat, M., Dafalias, Y. F. and Peek, R. (2010a), 'A destructuration theory and its application to SANICLAY model', *International Journal for Numerical and Analytical Methods in Geomechanics* **34**(10), 1009–1040.
- Taiebat, M., Jeremić, B., Dafalias, Y. F., Kaynia, A. M. and Cheng, Z. (2010b), 'Propagation of seismic waves through liquefied soils', *Soil Dynamics and Earthquake Engineering* **30**(4), 236–257.
- Verdugo, R. and Ishihara, K. (1996), 'The steady state of sandy soils', *Soils and Foundations* **36**(2), 81–91.
- Vucetic, M. and Dobry, R. (1991), 'Effect of soil plasticity on cyclic response', *Journal of Geotechnical Engineering* **117**(1), 89–107.
- Wood, D. M. (1974), Some Aspects of the Mechanical Behaviour of Kaolin under Truly Triaxial Conditions of Stress and Strain., PhD thesis, University of Cambridge.
- Yamada, Y. and Ishihara, K. (1983), 'Undrained deformation characteristics of sand in multi-directional shear', *Soils and Foundations* **23**(1), 61–79.
- Yasuhara, K., Hirao, K. and Hyde, A. (1992), 'Effects of cyclic loading on undrained strength and compressibility of clay', *Soils and Foundations* **32**(1), 100–116.
- Yoshimine, M., Ishihara, K. and Vargas, W. (1998), 'Effects of principal stress direction and intermediate principal stress on drained shear behavior of sand', *Soils and Foundations* **38**(3), 177–186.
- Zergoun, M. and Vaid, Y. (1994), 'Effective stress response of clay to undrained cyclic loading', *Canadian Geotechnical Journal* **31**(5), 714–727.